

# INTRODUCTION



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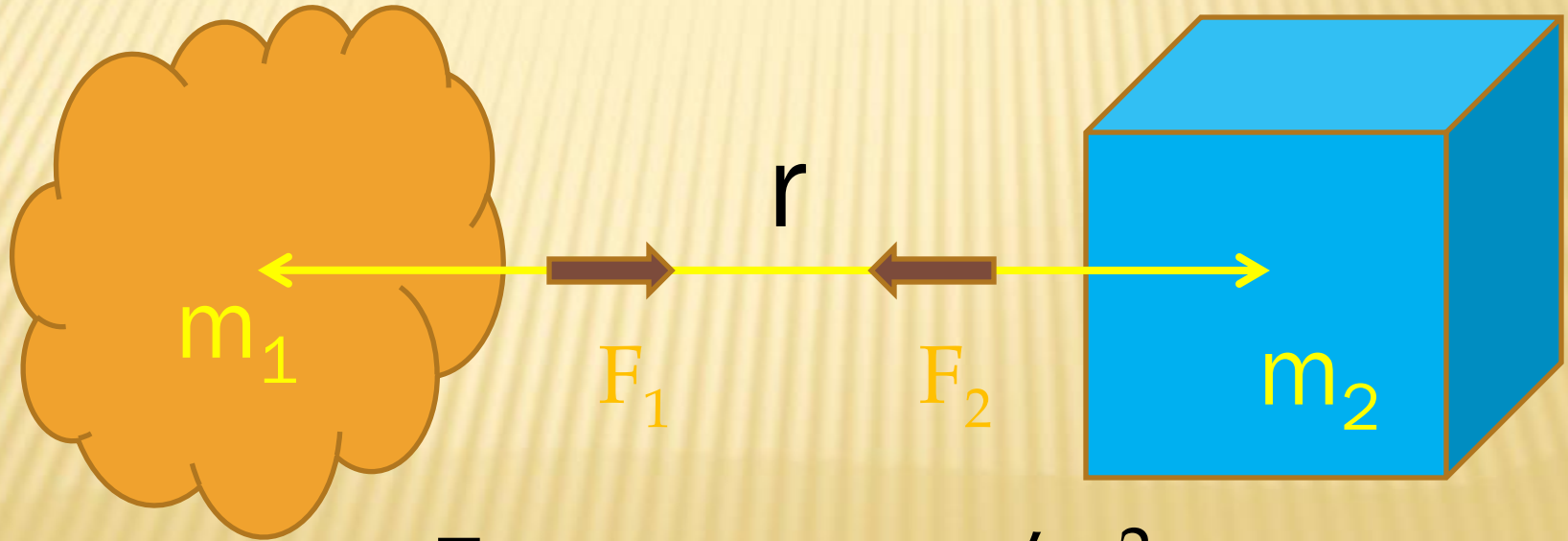


# NEWTON'S LAW OF GRAVITATION

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**Statement :** Every particle attracts every other particle in the universe with a force that is directly proportional to the product of their masses and inversely proportional to the square of the distance between their centers.

The law states that every point mass attracts every other point mass by a force acting along the line intersecting the two points.



$$F \propto m_1 \cdot m_2 / r^2$$

$$F \propto m_1 \cdot m_2 / r^2 \quad F = G m_1 \cdot m_2 / r^2$$

$$G = F \cdot r^2 / m_1 \cdot m_2 \dots\dots (1)$$

G - Gravitational Constant

**Unit of G - N . m<sup>2</sup> / Kg<sup>2</sup>**

$$F = m \cdot a, \quad a = dv/dt, \quad v = dx/dt$$

$$F = \text{Kg} \cdot \text{M} / \text{sec}^2$$

$$[F] = [M^1 L^1 T^{-2}]$$

$$[r^2] = [M^0 L^2 T^0]$$

$$[m_1 \cdot m_2] = [M^2 L^0 T^0]$$

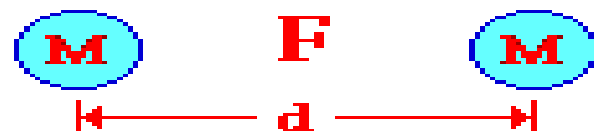
$$[G] = [M^{1-2} L^{1+2} T^{-2}]$$

**Dimensions of G**

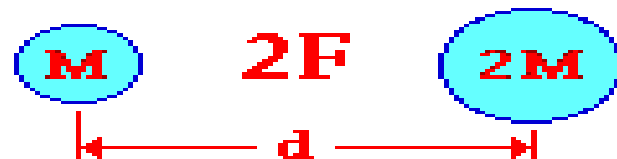
$$[G] = [M^{-1} L^3 T^{-2}]$$

## Effect of Mass on $F_{\text{grav}}$

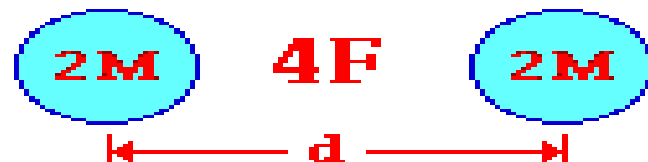
attract with a force of



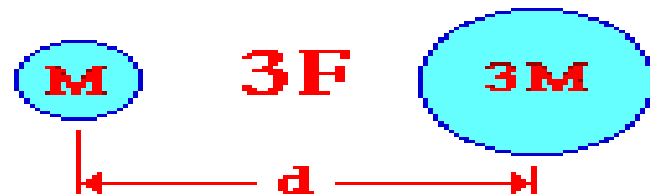
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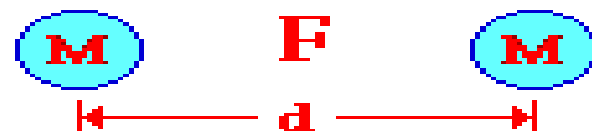


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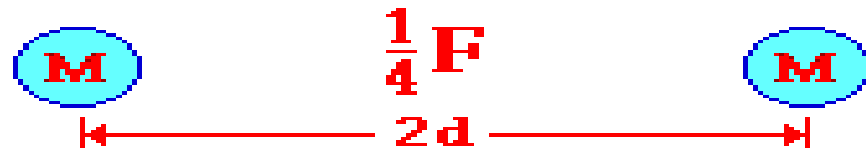


## Effect of Distance on $F_{\text{grav}}$

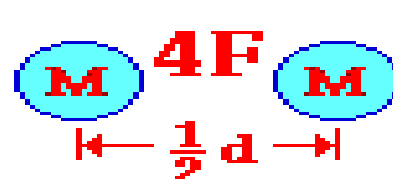
attract with a force of



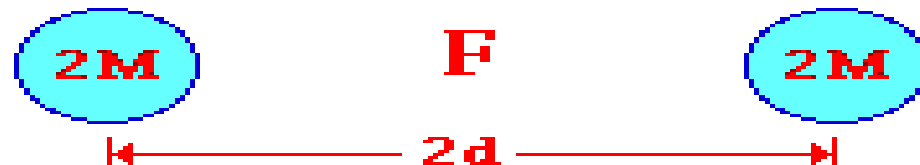
attract with a force of



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# GRAVITATIONAL FIELD

The area around the body within which the force of attraction is applicable is called Gravitational Field.

The Intensity or strength of the Gravitational Field at a point is defined as the force experienced by a unit mass at that point.

$$F \propto M \cdot m / r^2$$

$$F = - G M \cdot m / r^2$$

For  $M = 1$

$$F = - G \cdot m / r^2$$

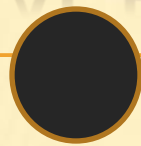
# GRAVITATIONAL POTENTIAL



Force of Attraction Decreases  
Force of Attraction Increases

The potential energy is equal to the amount of energy required to bring the unit mass from the area of no gravitational force present.

# GRAVITATIONAL POTENTIAL OF MASS M



x

0

A

dx

B

$$F = -G m . M / x^2$$

$$F = -G m . 1 / x^2$$

$$F = -G m / x^2$$

$$\text{Work Done} = \text{Force} . \text{Displacement} \quad [\text{From B to A}]$$

$$= -G m / x^2 . dx$$

$$= - \int G m / x^2 . = - \int G m x^{-2} dx$$

$V = -G m / r$  [ Is the potential at distance r. The potential difference at infinite distance  $V=0$ . ]



# GRAVITATIONAL POTENTIAL ( V )

The work done in bringing a unit mass from the given point to infinity against gravitational force of attraction.

$$V = - G \ m / x$$

**m** – mass of the ring

**x** - distance

# GRAVITATIONAL FIELD

The area around the body within which the force of attraction is applicable is called Gravitational Field.

## GRAVITATIONAL FIELD INTENSITY ( E )

The Intensity or strength of the Gravitational Field at a point is defined as the force experienced by a unit mass at that point.

$$E = - dV/dr, \quad V - \text{Gravitational Potential}$$

$r$  - distance

# FORMULIES SOLID SPHERE

$$V = -G \frac{m}{x} \quad \& \quad E = -dV/dx$$

Density = **Mass**/Volume ( Total Surface Area)

$$\rho = \mathbf{M}/V$$

$$\mathbf{M} = \rho V$$

Volume  $V = \text{Area} \times \text{Thickness}$

Area =  $4 \pi x^2$  , Thickness =  $dx$

$$V = 4 \pi x^2 \cdot dx$$

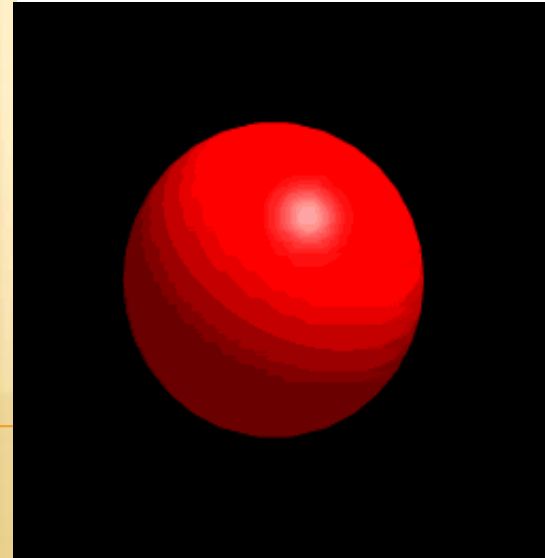
$$\mathbf{M} = \rho 4 \pi x^2 \cdot Dx, \int x dx = x^2 / 2, dx^2/dx = x^1$$

# SOLID SPHERE

At a point **out** side the Solid Sphere.

At a point **In**Side the Solid Sphere.

At a point **on** the Solid Sphere.

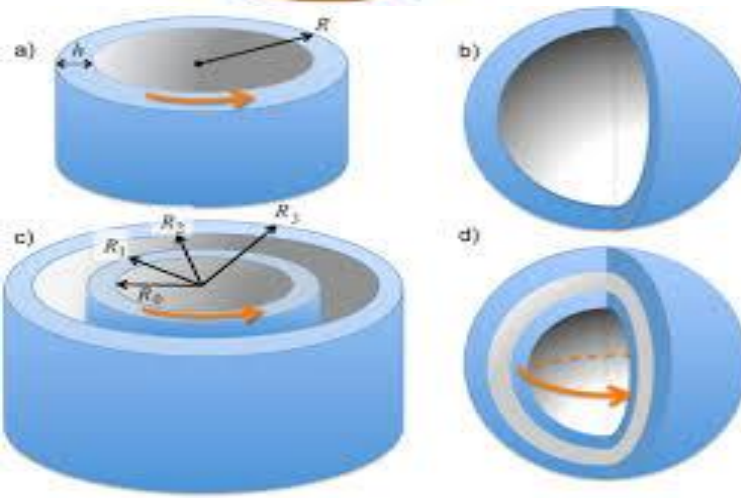
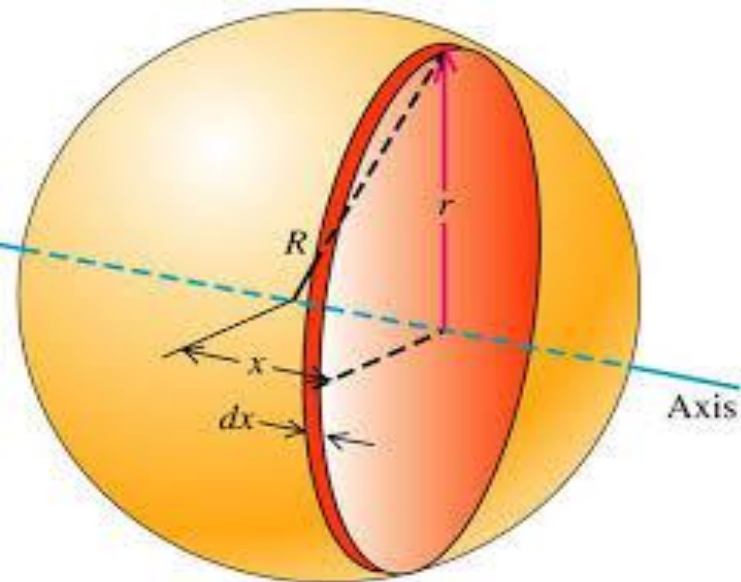


# Spherical Shell

At a point **out side** the Spherical Shell.

At a point **In side** the Spherical Shell.

At a point **on** the Spherical Shell.



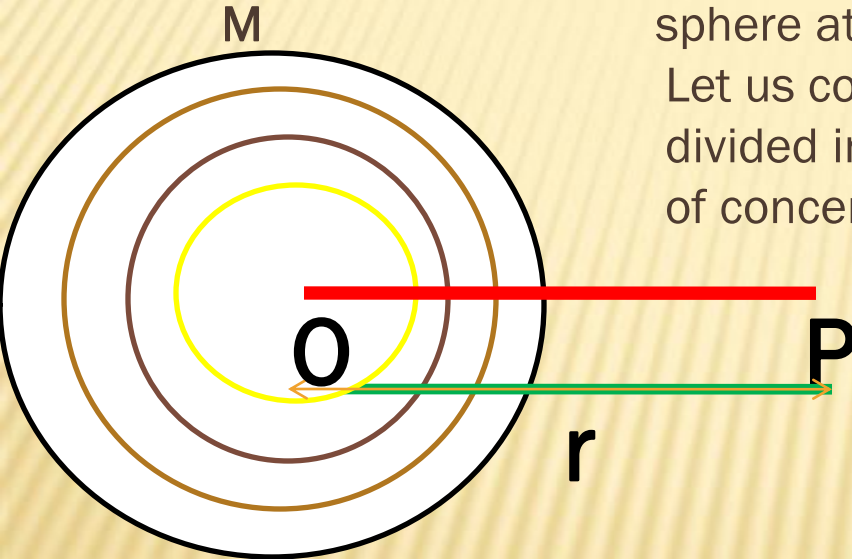


# SOLID SPHERE – POINT OUTSIDE

Consider point P is outside to solid sphere at a distance  $r$  from centre O.

Let us consider the solid sphere is divided into large number of concentric spheres of

masses  $m_1, m_2, m_3, \dots$



$$V = -G \frac{m}{r}$$

$$V = -G \frac{m_1}{r} +$$

$$-G \frac{m_2}{r} +$$

$$-G \frac{m_3}{r} + \dots$$

$$V = -G \frac{M}{r} \quad [m_1 + m_2 + m_3 + \dots = M]$$

G ( $6.673 \times 10^{-11} \text{ N m}^2/\text{kg}^2$ ),  $m_1$  ( $5.98 \times 10^{24} \text{ kg}$ ),  $m_2$  (70 kg) and  $d$  ( $6.38 \times 10^6 \text{ m}$ ) into the universal gravitation equation and solving for  $F_{\text{grav}}$ . The solu

$$F_{\text{grav}} = \frac{(6.673 \times 10^{-11} \text{ N m}^2/\text{kg}^2) \cdot (5.98 \times 10^{24} \text{ kg}) \cdot (70 \text{ kg})}{(6.38 \times 10^6 \text{ m})^2}$$

$$F_{\text{grav}} = 686 \text{ N}$$

So  $F_{\text{grav}} = \frac{(6.673 \times 10^{-11} \text{ N m}^2/\text{kg}^2) \cdot (5.98 \times 10^{24} \text{ kg}) \cdot (70 \text{ kg})}{(6.39 \times 10^6 \text{ m})^2}$

$$F_{\text{grav}} = 684 \text{ N}$$

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# The Universality of Gravity

Gravitational interactions do not simply exist between the earth and other objects; and not simply between the sun and other planets. Gr

	Mass of Object 1(kg)	Mass of Object 2 (kg)	Separation Distance (m)	Force of Gravity (N)
a.	Football Player100 kg	Earth 5.98 x10 <sup>24</sup> kg	6.38 x 10 <sup>6</sup> m (on surface)	
b.	Ballerina40 kg	Earth 5.98 x10 <sup>24</sup> kg	6.38 x 10 <sup>6</sup> m (on surface)	
c.	Physics Student 70 kg	Earth 5.98 x10 <sup>24</sup> kg	6.60 x 10 <sup>6</sup> m (low-height orbit)	
d.	Physics Student70 kg	Physics Student 70 kg	1 m	
e.	Physics Student70 kg	Physics Student 70 kg	0.2 m	
f.	Physics Student70 kg	Physics Book 1 kg	1 m	
1	Physics 2	392 Moon 7.34 x10 <sup>22</sup> kg	4	1.37 x 10 <sup>16</sup> m/s the power -7
5	8	17	x 10 <sup>-6</sup>	6